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*Variation and Enrichment*

The parametrized 2-category constructions  $\text{Fib}/S$ , for  $S$  with finite limits, and  $W\text{-cat}$ , for  $W$  a bicategory, are further unified by considering, for fixed  $W$ , the 2-category of pseudo-functors  $H: A \rightarrow W$  which are locally discrete fibrations. This 2-category is biequivalently described as a 2-category whose objects are lax-functors  $W^{co} \rightarrow \text{mat}$ , where  $\text{mat}$  is the bicategory whose objects are sets and whose hom-categories are given by  $\text{mat}(X, A) = \text{set}^{A \times X}$ . The biequivalence is a direct generalization of the Grothendieck biequivalence between fibrations and  $\text{CAT}$ -valued pseudo-functors and is mediated by pulling back a universal local discrete fibration  $\text{mat}_* \rightarrow \text{mat}$ . Further, the 2-category is also biequivalent to the classical  $\hat{W}\text{-cat}$ , where  $\hat{W}$  is the bicategory whose objects are those of  $W$  with  $\hat{W}(w, x) = \text{set}^{W(w, x)^{op}}$ . We will show how to recover the usual variable and enriched categories within this framework.

Work with JRB Cockett and SB Niefield.