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Some Turan and anti-Ramsey numbers

Let G be a graph obtained by adding a chord to a cycle, and let $C(G)$ be the set of cycles which are subgraphs of G . Here we study the relation between $\text{ex}(n, C(G))$ and $f(n, G)$, where $\text{ex}(n, C(G))$ is the maximum number of edges of a graph on n vertices with no subgraph isomorphic to an element of $C(G)$; and $f(n, G)$ is the minimum integer k such that for every edge-coloring of the complete graph of order n which uses exactly k colors, there is at least one copy of G all whose edges have different colors.

In particular we show that if G is the diamond (C_4 with a chord), then

$$\text{ex}(n, \{C_3, C_4\}) + 2 \leq f(n, G) \leq \text{ex}(n, \{C_3, C_4\}) + (n + 1).$$