${\bf GALIA\ DAFNI},\ {\bf Concordia\ University},\ 1455\ {\bf de\ Maisonneuve\ Blvd}.\ {\bf West},\ {\bf Montreal},\ {\bf Quebec\ H3G\ 1M8} \ {\bf An\ atomic\ decomposition\ of\ the\ Hajlasz\ Sobolev\ space\ M_1^1\ on\ manifolds}$ 

We compare several possible notions of Hardy–Sobolev spaces on a manifold with a doubling measure. In particular, we consider several characterizations of these spaces, in terms of maximal functions, atomic decompositions, and gradients, and apply them to the  $L^1$  Sobolev space  $M_1^1$ , defined by Hajlasz. Joint work with N. Badr.