Problem 1/9. An $m \times n$ grid is placed so that it has it's corners at (0,0) and (m,n). A legal move is defined as a move either one unit in the positive y direction or one unit in the positive x direction. The point (i, j), where $0 \le i \le m$ and $0 \le j \le n$, is removed from the grid so that it is no longer possible to pass through this point on the way to (m, n). How many possible paths are there from (0, 0) to (m, n)?

Problem 2/9. Given a point P and two straight line segments on a rectangular piece of paper in such a way that the intersection point Q of the straight lines does not lie on the paper. How can we construct the straight line PQ with the help of a ruler if we are allowed to draw only within the limits of the paper?

Problem 3/9. A convex polygon has 1993 vertices which are colored so that neighboring vertices are of different colors. Prove that one can divide the polygon into triangles with non-intersecting diagonals whose endpoints are of different colors.

Problem 4/9. A triangle is called Heronian if its sides and area are integers. Determine all five Heronian triangles whose perimeter is numerically the same as its area.

Problem 5/9. A set of five "Trick Math Cubes" is shown schematically on the right. A "magician" asks you to roll them and to add the five numbers on top of them. He starts adding them at the same time, and writes down the correct answer on a piece of paper long before you are finished with the task. How does he do it? Expose and explain this trick.

